

Test I

9/16/02

Math 184H

Name_____

Show all work to obtain full credit!

1. Evaluate.

$$(a) \lim_{x \rightarrow -1} \frac{x^2 - 1}{x + 1} =$$

$$(b) \lim_{x \rightarrow 1} (4x^3 - 2x - 7) =$$

$$(c) \lim_{x \rightarrow -\infty} \frac{2x^3 - 5x^2 + 7x - 9}{5x^3 - 6x + 11} =$$

$$(d) \lim_{x \rightarrow 0} \frac{x}{\sqrt{x + 4} - 2} =$$

$$(e) \lim_{x \rightarrow -2^+} \frac{|x^2 - 4|}{x^2 + 3x + 2} =$$

$$(f) \lim_{x \rightarrow 2^+} 3\sqrt{2-x} =$$

$$(g) \lim_{x \rightarrow -\infty} \frac{3x^3 - 15x^2 - 9x}{5x^7 + x - 8} =$$

$$(h) \lim_{x \rightarrow 1^-} \frac{2}{x-1} =$$

$$(i) \lim_{x \rightarrow -1^-} \frac{|x+1|}{x+1} =$$

2. Sketch the graph of $y = f(x)$ and find $\lim_{x \rightarrow 2} f(x)$ where $f(x) = \begin{cases} 2x & \text{if } x \leq -2 \\ x^2 - 1 & \text{if } x \in (-2, 1] \\ 3x + 1 & \text{if } x \geq 1 \end{cases}$.

3. Use the Intermediate Value Theorem to verify that $f(x) = x^3 - 4x - 2$ has a zero in the interval $[-2, -1]$.

4. Find all discontinuities of $f(x) = \frac{\tan x}{x}$. For each discontinuity that is removable, define a new function that removes the discontinuity.

5. Use the definition of the limit to prove that the following limits exist.

(a) $\lim_{x \rightarrow 1} (x^2 - x + 1) = 1$

(b) $\lim_{x \rightarrow 1} \frac{x + 2}{x^2} =$